

1. Find the area under the graph of
- $y = 3\sqrt{x}$
- between
- $x = 0$
- and
- $x = 9$
- .

$$\int_0^9 3\sqrt{x} dx = \int_0^9 3x^{1/2} dx = \left[3 \frac{x^{3/2}}{3/2} \right]_0^9 = \left[2\sqrt{x^3} \right]_0^9 = 2\sqrt{9^3} - 2\sqrt{0^3} = 2 \cdot 3^3 = \boxed{54 \text{ sq units}}$$

$$2. \int_0^1 \frac{1}{\sqrt{1-x^2}} dx = \left[\sin^{-1}(x) \right]_0^1 = \sin^{-1}(1) - \sin^{-1}(0) = \frac{\pi}{2} - 0 = \boxed{\frac{\pi}{2}}$$

$$3. \int_0^2 \left(\frac{x^2}{3} + 2x + 1 \right) dx = \left[\frac{x^3}{9} + x^2 + x \right]_0^2 = \left(\frac{2^3}{9} + 2^2 + 2 \right) - \left(\frac{0^3}{9} + 0^2 + 0 \right)$$

$$= \frac{8}{9} + 6 = \frac{8}{9} + \frac{54}{9} = \boxed{\frac{62}{9}}$$

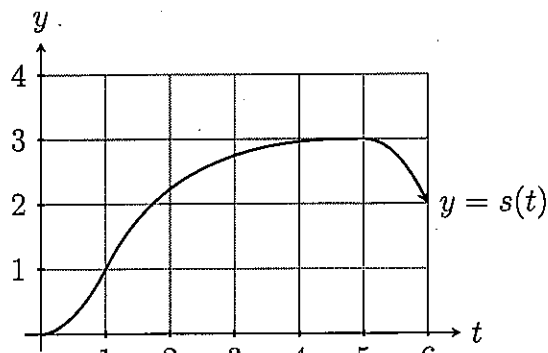
4. Find the derivative of the function
- $F(x) = \int_1^x \frac{t^5 + \sin(\pi t)}{e^t} dt$
- .

By FTC I,
$$F'(x) = \frac{x^5 + \sin(\pi x)}{e^x}$$

5. An object moving on a line has position
- $s(t)$
- and velocity
- $v(t)$
- at time
- t
- .
-
- The position function
- $s(t)$
- is graphed below.

$$(a) \int_5^6 v(t) dt = \left[s(t) \right]_5^6 = s(6) - s(5)$$

$$= 2 - 3 = \boxed{-1}$$



- (b) What does your answer to part (a) mean?

At time $t=6$, object is one unit left of where it was at time 5.

1. Find the derivative of the function
- $F(x) = \int_1^x \frac{\cos(t) \ln(t^2 + 7)}{t^5 + e^t} dt$
- .

By FTC I,
$$F'(x) = \frac{\cos(x) \ln(x^2 + 7)}{x^5 + e^x}$$

2.
$$\int_1^4 \frac{1}{\sqrt{x}} dx = \int_1^4 x^{-1/2} dx = \left[\frac{x^{1/2}}{1/2} \right]_1^4 = \left[2\sqrt{x} \right]_1^4 = 2\sqrt{4} - 2\sqrt{1} = 2 \cdot 2 - 2 = \boxed{2}$$

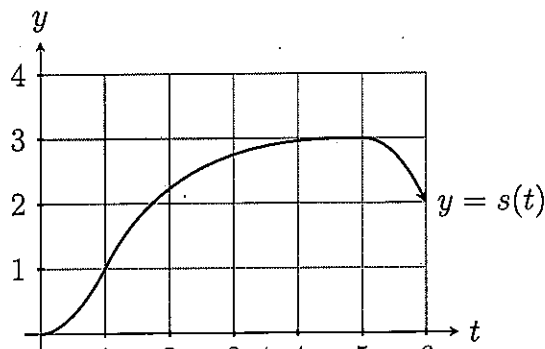
3.
$$\int_0^1 \frac{1}{1+x^2} dx = \left[\tan^{-1}(x) \right]_0^1 = \tan^{-1}(1) - \tan^{-1}(0) = \frac{\pi}{4} - 0 = \boxed{\frac{\pi}{4}}$$

4. Find the area under the graph of
- $y = x^3 + 1$
- between
- $x = 0$
- and
- $x = 2$
- .

$$A = \int_0^2 x^3 + 1 dx = \left[\frac{x^4}{4} + x \right]_0^2 = \left(\frac{2^4}{4} + 2 \right) - \left(\frac{0^4}{4} + 0 \right) = \frac{16}{4} + 2 = 4 + 2 = \boxed{6 \text{ sq. units}}$$

5. An object moving on a line has position
- $s(t)$
- and velocity
- $v(t)$
- at time
- t
- .
-
- The position function
- $s(t)$
- is graphed below.

(a)
$$\int_1^6 v(t) dt = \left[s(t) \right]_1^6 = s(6) - s(1) = 2 - 1 = \boxed{1}$$



- (b) What does your answer to part (a) mean?

At time $t=6$, object is one unit to right of where it was at time $t=1$.