

1. (7 pts.) Find all values of x at which the tangent line to $f(x) = 2 + e^x - x$ is horizontal.

Need to solve $f'(x) = 0$

$$0 + e^x - 1 = 0$$

$$e^x = 1$$

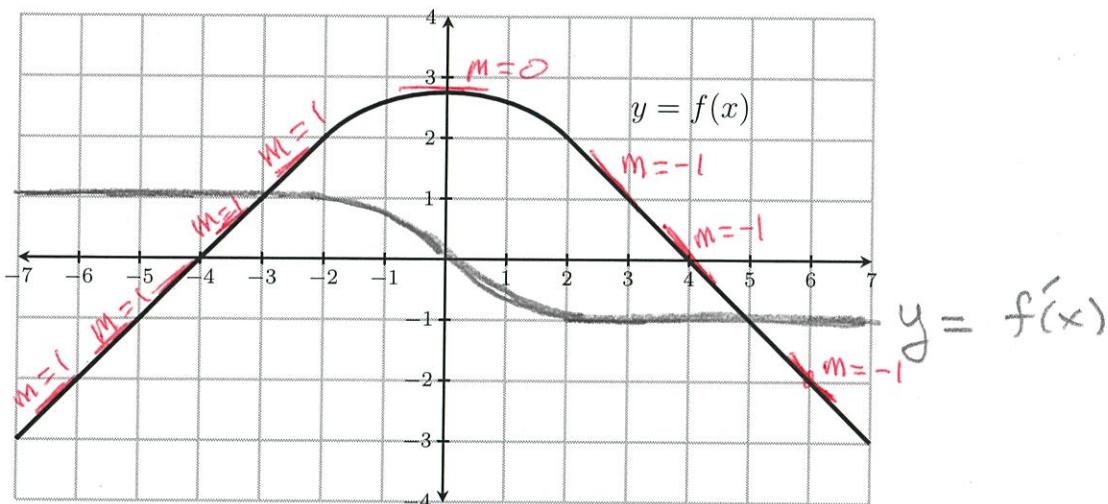
$$\ln(e^x) = \ln(1)$$

$$x = 0$$

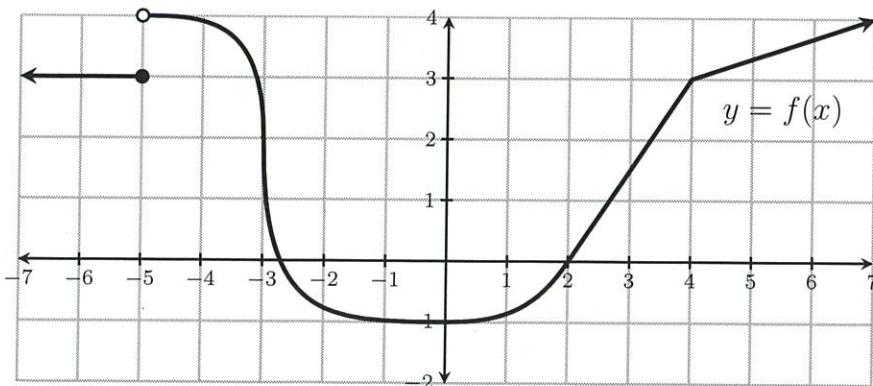
Tangent line to $y = f(x)$ is horizontal only at $x = 0$

2. (7 pts.) The graph of a function $f(x)$ is shown below.

Using the same coordinate axis, sketch the graph of its derivative $f'(x)$



3. (6 pts.) This problem concerns the function $f(x)$ sketched below.



vertical tangent
cusp

- (a) State the x -values at which f is not continuous.

- (b) State the x -values at which f is not differentiable.

$x = -5$
 $x = -5, x = -3, x = 4$

f not continuous



1. (7 pts.) Find all values of x at which the tangent line to $f(x) = \frac{x}{e} - e^x$ is horizontal.

Need to solve $f'(x) = 0$

$$\frac{1}{e} - e^x = 0$$

$$e^x = \frac{1}{e}$$

$$\ln(e^x) = \ln\left(\frac{1}{e}\right)$$

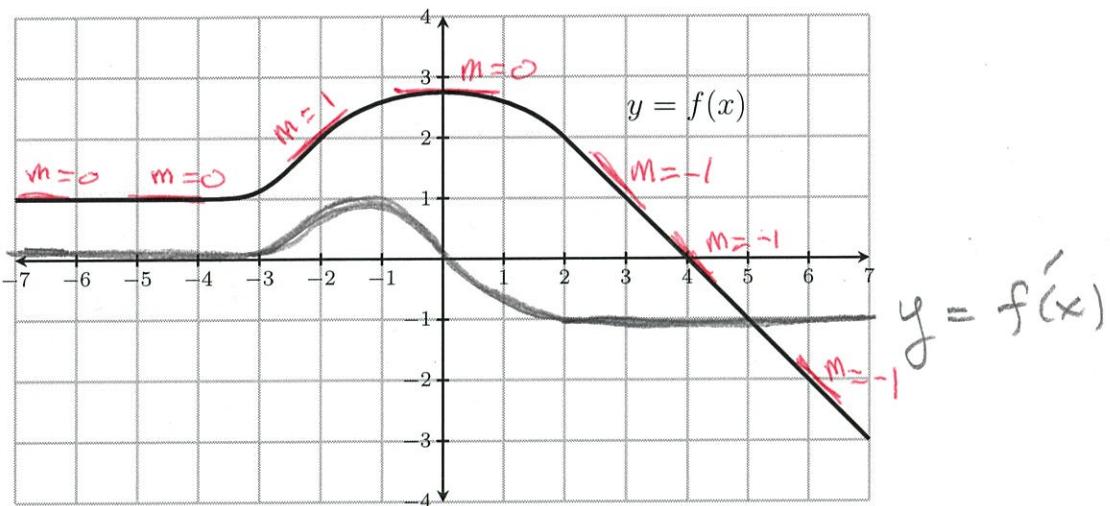
$$x = -1$$

$\left\{ f(x) = \frac{1}{e}x - e^x \right.$

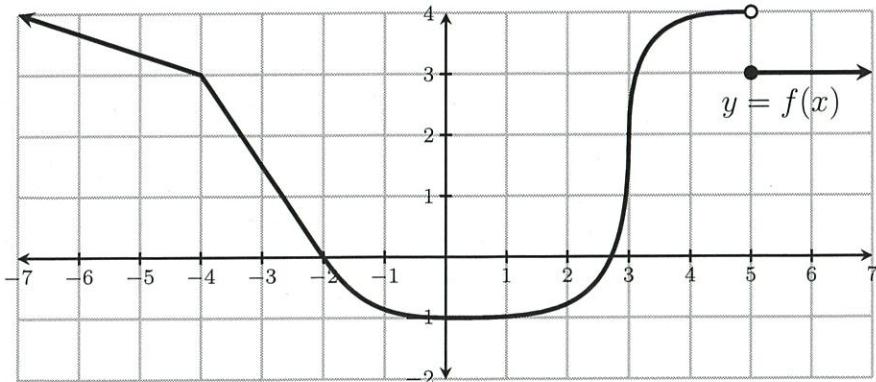
Tangent line to $y = f(x)$
is horizontal only
at $x = -1$

2. (7 pts.) The graph of a function $f(x)$ is shown below.

Using the same coordinate axis, sketch the graph of its derivative $f'(x)$



3. (6 pts.) This problem concerns the function $f(x)$ sketched below.



f not continuous
(vertical tangent)
 $x = 5$
 $x = -4, x = 3, x = 5$

- (a) State the x -values at which f is not continuous.

- (b) State the x -values at which f is not differentiable.

CUSP