

1. Complete the truth tables.

(a) 

| P | Q | $P \vee Q$ |
|---|---|------------|
| T | T | T          |
| T | F | T          |
| F | T | T          |
| F | F | F          |

(b) 

| P | Q | $P \wedge Q$ |
|---|---|--------------|
| T | T | T            |
| T | F | F            |
| F | T | F            |
| F | F | F            |

(c) 

| P | Q | $P \Rightarrow Q$ |
|---|---|-------------------|
| T | T | T                 |
| T | F | F                 |
| F | T | T                 |
| F | F | T                 |

(d) 

| P | Q | $P \Leftrightarrow Q$ |
|---|---|-----------------------|
| T | T | T                     |
| T | F | F                     |
| F | T | F                     |
| F | F | T                     |

2. Without changing its meaning, convert each sentence to a sentence of form "If P, then Q."

(a) Whenever a number is divisible by 4, it is even.

*If a number is divisible by 4, then it is even.*

(b) A function is continuous provided that it is differentiable.

*If a function is differentiable, then it is continuous.*

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(a) 

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(d) 

| P | Q | $P \Leftrightarrow Q$ |
|---|---|-----------------------|
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2. Without changing its meaning, convert each sentence to a sentence of form "If P, then Q."

(a) You use an umbrella only if it is raining.

*If you use an umbrella, then it is raining.*

(b) Whenever you are lost, consult a map.

*If you are lost, then use a map.*

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|---|---|-------------------|
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| F | F | T                 |

| P | Q | $P \wedge Q$ |
|---|---|--------------|
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| P | Q | $P \Leftrightarrow Q$ |
|---|---|-----------------------|
| T | T | T                     |
| T | F | F                     |
| F | T | F                     |
| F | F | T                     |

2. Without changing its meaning, convert each sentence to a sentence of form "If  $P$ , then  $Q$ ."

(a) The quadratic formula applies provided that you are solving a quadratic equation.

If you are solving a quadratic equation, then the quadratic formula applies.

(b) Work carefully whenever you take a quiz.

If you take a quiz, then work carefully.

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| P | Q | $P \wedge Q$ |
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| P | Q | $P \Rightarrow Q$ |
|---|---|-------------------|
| T | T | T                 |
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| P | Q | $P \Leftrightarrow Q$ |
|---|---|-----------------------|
| T | T | T                     |
| T | F | F                     |
| F | T | F                     |
| F | F | T                     |

2. Without changing its meaning, convert each sentence to a sentence of form "If  $P$ , then  $Q$ ."

(a) For a number to be even, it is sufficient that it be a multiple of 4.

If a number is a multiple of 4, then it is even.

(b) Whenever the derivative of a function is zero, the function is a constant function.

If the derivative of a function is zero, then the function is a constant function.